

Take out the two homework pages from last class.

Make sure you put your name on them :)

# INTRODUCTION TO RATIOS

GUIDED NOTES

## IMPORTANT VOCABULARY:

- **Ratios:** A Comparison of two quantities

## INTRODUCTION TO RATIOS

1. Ratios can be part-to-part,  
parts-to-whole or whole-to-part comparisons.
2. There are three ways to write ratios:  
fraction, "to" and  
colon :
3. The ratio of a to b can be written as:  $\frac{a}{b}$ , a to b, a : b

## GUIDED PRACTICE

In class, there are 12 girls and 11 boys. Write each ratio 3 ways.

- **Girls to boys**  
 $\frac{12}{11}$     12 to 11    12 : 11

- **Boys to girls**  
 $\frac{11}{12}$     11 to 12    11 : 12

Suppose you are at camp. There are 5 counselors and 13 campers in every cabin. Write each ratio 3 ways. TOTAL 18

- **Counselors to campers**  
 $\frac{5}{13}$     5 to 13    5 : 13
- **Campers to total people in the cabin**  
 $\frac{13}{18}$     13 to 18    13 : 18

There are three times as many cashews as almonds in the mixture of nuts. Write each ratio 3 ways.

- **Cashews to almonds**  
 $\frac{3}{1}$     3 to 1    3 : 1

- **Almonds to cashews**  
 $\frac{1}{3}$     1 to 3    1 : 3

Write a ratio in three ways for each statement:

- There are 125 students for every 5 teachers  
 $\frac{125}{5}$     125 to 5    125 : 5

- Combine 1 part ginger ale to 4 parts fruit punch  
 $\frac{1}{4}$     1 to 4    1 : 4

Name: \_\_\_\_\_

Date: \_\_\_\_\_



# INTRODUCTION TO RATIOS

## PRACTICE PROBLEMS

Write each ratio 3 ways

<p>#1 There are 5 cats for every 4 dogs at the animal shelter. (What is the ratio of dogs to cats?)</p> <p><math>\frac{4}{5}</math>    4 to 5    4:5</p>	<p>#2 In band, there are 3 woodwinds for every 1 percussion player. (What is the ratio of woodwinds to percussion players?)</p> <p><math>\frac{3}{1}</math>    3 to 1    3:1</p>
<p>#3 In Kelsey's pencil case, she has 2 highlighters for every 7 pencils. (What is the ratio of pencils to highlighters?)</p> <p><math>\frac{7}{2}</math>    7 to 2    7:2</p>	<p>#4 In the bag, there are 19 green marbles for every 11 blue marbles. (What is the ratio of green marbles to total (30) marbles?)</p> <p><math>\frac{19}{30}</math>    19 to 30    19:30</p>

$$\begin{array}{r} 19 \\ +11 \\ \hline 30 \end{array}$$

<p>#5 At the aquarium, there are 200 fish for every 1 shark. (What is the ratio of sharks to fish?)</p> <p><math>\frac{1}{200}</math>    1 to 200    1:200</p>	<p>#6 The recipe calls for 2 cups of flour for every cup of sugar. (What is the ratio of sugar to flour?)</p> <p><math>\frac{1}{2}</math>    1 to 2    1:2</p>
<p>#7 Each supply bin has 4 bottles of glue and 3 pairs of scissors. (What is the ratio of total supplies to bottles of glue?)</p> <p><math>3 + 4 = 7</math></p> <p><math>\frac{7}{4}</math>    7 to 4    7:4</p>	<p>#8 Last year Anna read 20 books. 5 were non-fiction, 7 were graphic novels and 8 were mystery novels. (What is the ratio of graphic novels to total books?)</p> <p><math>\frac{7}{20}</math>    7:20    7 to 20</p>

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**RATIOS AS FRACTIONS**  
**N-GEN MATH® 6**

**Guided Notes**

In the last lesson few lessons, we have worked with ratios in various ways. Remember that ratios are simply a comparison of how much of one thing there is compared to another. We want to express this in a simple way. A **mathematical notation** has been invented to do so.

**SHOWING RATIOS WITH COLONS**

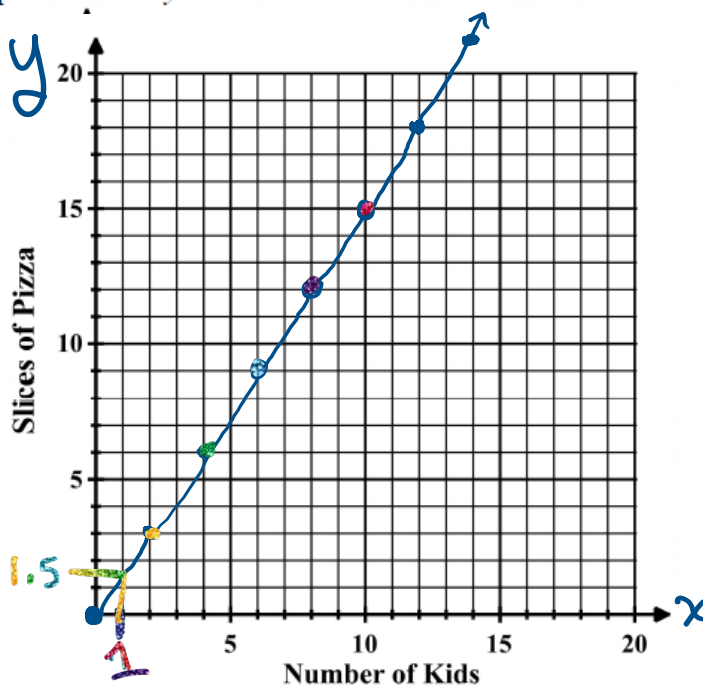
If we have a quantity of  $a$  and a quantity of  $b$  then the ratio of  $a$  to  $b$  is shown as:  $a:b$ .

**Exercise #1:** At a birthday party, the ratio of pizza slices to kids is  $3:2$ .

(a) If there are 12 kids, how many pizza slices are there? Fill in the table below to justify your answer.

Kids	0	2	4	6	8	10	12	14
Slices	0	3	6	9	12	15	18	21

(b) Using your table from (a), make a plot of points on the grid where the number of kids is the  $x$ -coordinate and the number of slices of pizza is the  $y$ -coordinate.



(c) Connect these points with a straight line.

(d) According to the graph, how much pizza does a single kid get? How does this relate to the ratio?

Every kid gets 1.5 slices

$$\begin{array}{l}
 K \quad \frac{2}{3} \div 2 = \frac{1}{3} \\
 S \quad \frac{3}{2} \div 2 = \boxed{1.5}
 \end{array}$$

(e) At a larger party there are 30 kids. If the ratio of pizza slices to kids stays the same, how many pizza slices will be needed?

$$\begin{array}{l}
 K \quad \frac{2}{3} \times 15 = \frac{30}{3} \\
 S \quad \frac{3}{2} \times 15 = \boxed{45} \text{ slices}
 \end{array}$$

Besides representing ratios using phrases like “3 cats to 5 dogs” and the colon notation, 3:5, ratios are often represented by fractions. Let’s see why this makes sense.

**Exercise #2:** In a sixth-grade class 3 out of every 5 students have brown hair. The ratio of students with brown hair to all students, therefore, is 3:5 (3 to 5).

(a) Fill out the table below.

EQUIVALENT FRACTIONS

Brown Hair	<u>3</u>	<u>6</u>	<u>9</u>	<u>12</u>
All Students	5	10	15	20

(b) Form fractions from this table using the first row as the numerator and the second row as the denominator.

$$\frac{3}{5} > \frac{6}{10} > \frac{9}{15} > \frac{12}{20}$$

(c) What does each fraction reduce to?

$$\frac{3}{5}$$

(d) If there were 40 students in the class, how many would have brown hair based on this ratio? Fill in the missing numerator below.

B  $\frac{3}{5} = \frac{?}{40}$  24 students have brown hair  
 T  $\begin{matrix} \times 8 \\ \times 8 \end{matrix}$

### RATIOS AS FRACTIONS

The ratio of  $a$  to  $b$  (or  $a:b$ ) can be represented in fraction form as  $\frac{a}{b}$ . This fraction represents how much you would need to multiply  $b$  by to get  $a$ .

**Exercise #3:** The ratio of girls to boys on a coed soccer team is 4 to 3.

(a) Represent this ratio as a fraction.

$$\frac{4}{3}$$

(b) If there are 12 boys, how many girls are there? Show how you found your answer.

G  $\frac{4}{3} \times 4 = \frac{16}{3}$  girls  
 B  $\frac{4}{3} = \frac{16}{12}$

**Exercise #4:** In a popular cereal, the ratio of marshmallow pieces to wheat squares is 2:7. If Elliette’s cereal bowl contains 63 wheat squares, how many marshmallow pieces should it contain? Justify your answer.

m  $\frac{2}{7} \times 9 = \frac{18}{7}$  marshmallow pieces  
 w.s.  $\frac{2}{7} = \frac{18}{63}$

Name: \_\_\_\_\_

Date: \_\_\_\_\_

**RATIOS AS FRACTIONS**  
**N-GEN MATH® 6 HOMEWORK**

**FLUENCY**

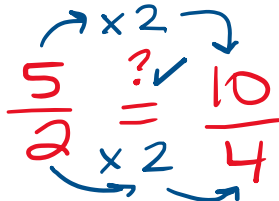
1. Which of the following is not a correct way to represent the ratio 5 to 2?

~~(1)  $\frac{2}{5}$~~

(3) 5:2

(2)  $\frac{5}{2}$

(4) 10:4



$\frac{5}{2}$  and  $\frac{10}{4}$  are EQUIVALENT.

2. The collection below contains parallelograms and triangles. Answer the following ratio questions about this collection of shapes.

(a) What is the ratio of triangles to parallelograms?



$\frac{3}{6}$ , 3 to 6  
3:6

$\frac{3}{6} = \frac{6}{12}$      $\frac{3}{6} = \frac{1}{2}$

(b) The ratio in (a) is equivalent to what fraction?

$\frac{3}{6} = \frac{1}{2}$

(c) If this collection was expanded so that there were 20 parallelograms (with the same ratio as before), how many triangles would there be?

$\frac{3}{6} = \frac{?}{20}$

$\frac{1}{2} \times 10 = \frac{10}{20}$   
 $\times 10$

(d) More challenging: If this collection was expanded so that there were 90 total shapes (with the same ratio as before), how many of them would be triangles? Explain.

$T + P = 90$   
 $3 + 6 = 9$

$30 + 60 = 90$

3. If the ratio of  $a$  to  $b$  is 10 to 3 then  $a$  is

(1)  $\frac{3}{10}$  of  $b$

(3) 10 times  $b$

$\frac{a}{b} = \frac{10}{3}$

(2)  $3\frac{1}{3}$  times  $b$

(4) 3 times  $b$



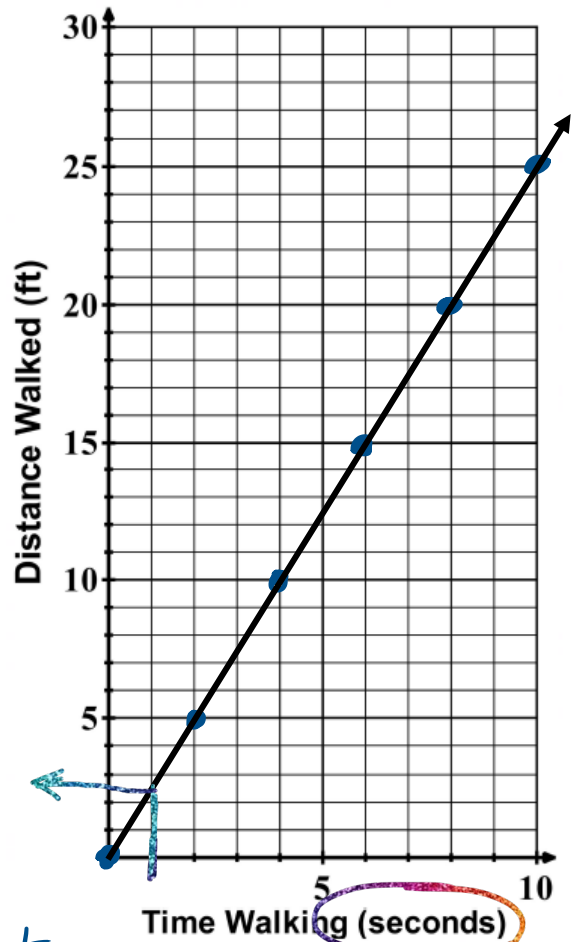
## USING YOUR MATH

4. Ava is walking at a constant speed where for every 5 feet it takes 2 seconds. So, the ratio of feet to seconds is 5 to 2.

- (a) Fill in the table below with times and distances.

Time (seconds)	Distance (feet)
0	0
2	5
4	10
6	15
8	20
10	25

- (b) Plot the rows of the table above on the grid paper, where the  $x$ -coordinate is time and the  $y$ -coordinate is distance. Connect with a straight line.



- (c) How many feet does Ava walk in one second? How does this relate to the ratio?

$\frac{5}{2} \div 2 = 2.5$   
 $\frac{5}{2} \div 2 = 1$   
1 second = 2.5 feet (Unit Rate)

5. In a group of people, for every 20 people, 7 of them have blue eyes.

- (a) Write the ratio of the number of people with blue eyes to the total number of people in fraction form.
- (b) If there are 100 total people, how many of them have blue eyes? Explain how you found your answer.

$$\frac{7}{20}$$

$$\frac{7}{20} \times 5 = \frac{35}{100}$$

